An Operating Model for the Integrated Pest Management of Great Lakes Sea Lampreys

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\textbf{Abstract:} Models of entire managed systems, known as operating models or management strategy evaluation (MSE) models, have been developed in recent years to more fully account for uncertainty in multiple steps of fishery management. Here we describe an operating model of sea lamprey management in the Great Lakes and use the model to compare alternative management strategies for sea lamprey control in Lake Michigan. Control of sea lampreys is mainly achieved through the application of chemical lampricides that target stream-dwelling larvae before they become parasites. The operating model simulated uncertainty due to process variation in larval population dynamics, the accuracy of population assessments used to direct selection of areas to be chemically treated, and the effectiveness of these treatments. We used the operating model to compare the performance of stream selection strategies that either rely on assessments to direct chemical treatments or eliminate the assessment process altogether by relying on prior but uncertain knowledge of stream-level sea lamprey growth rates to specify a fixed schedule for chemical treatments. The fixed schedule strategy led to a modest improvement in expected suppression of parasitic sea lamprey abundance over the assessment-based strategy so long as assessment cost savings were allocated to chemical treatment when assessment was not used to select streams for treatment. We also evaluated the sensitivity of the assessment-based strategy to differing but plausible levels of assessment uncertainty. A moderate reduction in assessment uncertainty led to a large increase in suppression of parasitic sea lamprey abundance for the assessment-based selection strategy, emphasizing the importance of both accurately measuring and reducing assessment uncertainty.

\textbf{INTRODUCTION}

Fishery management can benefit greatly from forecasts of the consequences of alternative management strategies that properly account for system uncertainty [1]. Many forms of uncertainty can affect decision making [2, 3], including uncertainty about ecological processes that govern population dynamics (process uncertainty), our inability to observe systems without error (measurement uncertainty), and the “disconnect” between an intended management action and what actually happens in the real world (implementation uncertainty). Until recently, technical challenges prevented explicitly considering these multiple sources of uncertainty for a particular fishery simultaneously. During the past 20 years, however, fisheries scientists, particularly in southern Africa, Australia, and in association with the International Whaling Commission, have successfully developed tools that take into account each of these types of uncertainties and they have been used to evaluate alternative fishery management strategies [4-6]. Their approach entails developing an “operating model” that includes three components: a system model of the fish stock and its associated fishery, an observation model that describes what information can be obtained about the fish stock and the fishery, and a management model that describes how management actions are implemented and their effects on the fishery. In Australia, this approach has been termed Management Strategy Evaluation, or MSE [7]; MSE-style analyses of commercial fishery harvest systems are now widely viewed as a valuable, perhaps even essential, tool for fishery management, especially since the FAO Technical Consultation on the Precautionary Approach to Capture Fisheries [6, 8-10].
Fishery management is not limited to capture fisheries, however, and uncertainty exists in other aspects of fishery management [11-13]. In the Laurentian Great Lakes, a critical management challenge is cost-effective control of the exotic sea lamprey Petromyzon marinus, which invaded the upper Great Lakes in the 1930s and devastated fish communities [14]. Today, sea lamprey populations are controlled through a bi-national Integrated Pest Management Program led by the Great Lakes Fishery Commission (GLFC). The integrated program reduces parasitic sea lamprey production by targeting larval habitats with chemical lampricides [15], as well as employing various measures to reduce the reproductive success of adult sea lampreys as they return to Great Lakes tributary streams to spawn [16-18]. Each year the GLFC decides how to allocate limited pest control resources for the lampricide program they have developed a management strategy that utilizes assessment information on larval sea lamprey abundance and distribution and stream selection in streams to target a set of streams for lampricide treatment each year [19, 20]. The performance of this management strategy can be affected by process, assessment, and implementation uncertainty, but until recently these uncertainties have been largely ignored. In this paper, we describe an operating model for sea lamprey control that incorporates these uncertainties and our use of the model to explore alternative assessment strategies for the stream selection process for lampricide control.

BACKGROUND ON THE MANAGEMENT SYSTEM

Adult sea lampreys migrate into streams tributary to the Great Lakes during spring and spawn from late May through July. After hatching, larval sea lampreys drift downstream, burrow in soft substrates, and become filter-feeding ammonocoetes. After 3-6 years spent in these habitats, most larvae begin metamorphosis, at which time they develop the feeding apparatus required for the parasitic life stage. Metamorphosed sea lampreys (called transformers during migration) migrate downstream to the lake in fall or spring where they feed on host teleost fishes for 12-18 months before maturing and completing their semelparous life cycle.

Most sea lamprey control is achieved through the periodic treatment of lotic and lentic habitats with the lampricides TFM (3-triflouromethyl-4-nitrophenol) and Bayluscide (2′,5-dichloro-4′-nitrosalicylanilide), respectively. For a given budget the maximum level of control will be achieved if lampricide applications are directed to streams with the greatest abundance of larval sea lampreys expected to metamorphose in a given year relative to the cost of lampricide treatment for that area [21]. An assessment program is required to determine which streams contain the greatest number of larval sea lampreys expected to metamorphose in each year [19, 20]. The current larval assessment program used to prioritize streams for treatment is costly relative to the overall funds available for pest management; in recent years, larval assessment has accounted for one quarter to one third of the total sea lamprey management budget. Despite the high level of investment by the GLFC, the population estimates obtained from this assessment program are highly uncertain [22, 23]. Furthermore, the magnitude of population reduction in a stream treated with lampricides, while often assumed to be 95% or greater, can vary considerably across locations and over time, in part depending on environmental conditions (e.g., stream discharge) at the time of treatment.

Sea lamprey control is carried out in the North American Great Lakes to allow both wild and stocked teleost fishes, especially trout and salmon, to survive in sufficient numbers to contribute to a viable fishery and spawning population. Thus the primary objective of sea lamprey control is to achieve target levels of abundance of larger, older host fishes (mainly salmonines). In our analysis, however, we use the forecasted abundance of adult sea lampreys as our measure of performance for management strategies. Because sea lamprey abundance is far below and host abundance is far above the historical levels observed prior to the implementation of the control program, we can reasonably assume that sea lamprey attacks on hosts and thus host survival will be proportional to sea lamprey abundance over the range of abundances relevant to this analysis – moderate numbers of additional sea lampreys are unlikely to experience significant effects of exploitative competition [24].

Here we describe how we incorporated uncertainties about sea lamprey population dynamics, assessment uncertainty, and implementation error into an operating model. We used the model to compare the performance of management strategies that either rely on larval assessment to direct selection of streams for chemical treatment or instead operate on a fixed-treatment schedule, thus eliminating the need for larval assessment. We also considered the influence of assessment uncertainty on this comparison. Surprisingly, there are few other evaluations where alternative choices about how to allocate budgetary resources between population assessment and other management actions have been assessed [25].

THE OPERATING MODEL

Overview

We developed a stochastic age-structured population model to forecast changes in future sea lamprey abundance for each of the Laurentian Great Lakes resulting from implementation of a particular pest management strategy. The model includes the full life cycle for the population of sea lampreys occupying the Great Lakes and tributary streams and forecasts changes in abundance over a 100-year time horizon. The model represents the sea lamprey life cycle as having the following stages: larval, transformer or metamorphosing, parasitic, and spawning-phase (Fig. 1). To simulate control of sea lamprey production through application of lampricides, the model represents larval populations at the level of individual stream reaches that are the spatial units of chemical control. Spawning-phase sea lampreys are allocated to stream reaches based on stream size and larval abundance, then produce age-0 recruits based on a stock-recruitment function, and subsequently die. The operating model also allows stream-level manipulation of adult spawning success to simulate adult control tactics such as trapping of migrating adults or barriers to restrict access to spawning habitats. However, we will not be considering management strategies that include adult control in this analysis. Existing physical barriers are implicitly included in the model because only stream habitats downstream of such barriers are included as candidate stream reaches for lampricide control.
Because larval sea lampreys typically remain in streams for multiple years, the age- and length-structured larval population (ages 0 through 6 years) in each stream is updated annually to account for natural mortality, removals due to lampricide treatment, and losses due to metamorphosis to the parasitic life stage. The larval sea lampreys that complete metamorphosis and are not removed via lampricide control are added to the parasitic population for the lake. This cohort of parasites becomes the spawning-phase population in the following year after losses due to parasitic-phase natural mortality. In addition to the larval populations in stream habitats, the model also represents alternative larval habitat areas (Appendix A). The model includes uncertainty in biological processes (recruitment and growth), assessment of larval populations, and implementation of lampricide control. Definitions for all model parameters are provided in Table 1.

The complete set of sea lamprey-producing streams for each Great Lake was explicitly represented, following the approach used by the GLFC (Gavin Christie, GLFC, Ann Arbor, MI, personal communication) in which large streams are divided into reaches for which independent lampricide treatment decisions can be made. We relied on an existing database (known as the Empiric Stream Treatment Ranking [ESTR] database, used by the GLFC to select streams for lampricide treatment) as a source of physical (stream lengths, widths, etc), biological (larval growth rates and growing season lengths), and economic (treatment costs) information for streams [19]. Below we describe the details of the operating model as it applies to each of the Great Lakes, and note areas where the model has stream-, lake-, or region-specific parameter values. The application of the model presented in this paper, however, is for Lake Michigan only (Fig. 2).

**Fig. (1).** A sea lamprey life history diagram, showing the movement from the lake to streams during the adult phase and the return to the lake as parasites. Transformers refers to sea lamprey individuals that have recently completed metamorphosis to the parasitic life stage. The numbers reference model equations in the text for the various demographic processes. Also depicted is emigration of age-0 sea lamprey larvae to lentic habitats, as described in Appendix A.

**Fig. (2).** A map of Lake Michigan showing (solid circles) the location of tributary streams and rivers that are regularly infested with sea lampreys and treated for control.

**Biological Model**

Adult sea lampreys do not home to natal streams [26], therefore spawning-phase sea lampreys were allocated to stream reaches based on two rules: i) the drainage area of the stream, as streams with the greatest discharge have been found to accommodate the largest number of spawning-
Table 1. Parameters, Their Assumed Values, and State Variables Used in the Operating Model for Sea Lamprey

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Assumed Value or Equation Where Calculated</th>
</tr>
</thead>
<tbody>
<tr>
<td>$i$</td>
<td>Stream reach</td>
<td>range varies by lake</td>
</tr>
<tr>
<td>$a$</td>
<td>Age of larvae</td>
<td>0-6</td>
</tr>
<tr>
<td>$b$</td>
<td>Length bin</td>
<td>1-9</td>
</tr>
<tr>
<td>$t$</td>
<td>Year</td>
<td>1-100</td>
</tr>
</tbody>
</table>

**Stream reach and “pool” characteristics**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Assumed Value or Equation Where Calculated</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D_i$</td>
<td>Drainage area</td>
<td>varies by reach</td>
</tr>
<tr>
<td>$A_i$</td>
<td>Larval habitat area</td>
<td>varies by reach</td>
</tr>
<tr>
<td>$v_i$</td>
<td>Length of stream</td>
<td>varies by reach</td>
</tr>
<tr>
<td>$w_i$</td>
<td>Mean width of stream</td>
<td>varies by reach</td>
</tr>
<tr>
<td>$H_{1i}$</td>
<td>Proportion of type I larval habitat</td>
<td>varies by reach</td>
</tr>
<tr>
<td>$H_{2i}$</td>
<td>Proportion of type II larval habitat</td>
<td>varies by reach</td>
</tr>
<tr>
<td>$r$</td>
<td>Habitat suitability scalar</td>
<td>0.38$^3$</td>
</tr>
</tbody>
</table>

**Sea lamprey life cycle simulation**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Assumed Value or Equation Where Calculated</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S_{i}$</td>
<td>Reach abundance of spawning-phase sea lamprey</td>
<td>equation 1</td>
</tr>
<tr>
<td>$S_{T}$</td>
<td>Lake-wide abundance of spawning-phase sea lamprey</td>
<td>equation 12</td>
</tr>
<tr>
<td>$P_i$</td>
<td>Lake-wide abundance of parasites</td>
<td>equation 11</td>
</tr>
<tr>
<td>$T_{i}$</td>
<td>Reach abundance of transformers</td>
<td>equation 8</td>
</tr>
<tr>
<td>$T_{^\hat{i}}$</td>
<td>Assessed abundance of transformers</td>
<td>equation 13</td>
</tr>
<tr>
<td>$L_{a,a}$</td>
<td>Reach abundance of larval sea lamprey (ammocoetes)</td>
<td>equations 9,10</td>
</tr>
<tr>
<td>$p_A$</td>
<td>Proportion allocated by area</td>
<td>0.5</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Ricker model parameter</td>
<td>4.346</td>
</tr>
<tr>
<td>$\beta$</td>
<td>Ricker model parameter</td>
<td>0.1573</td>
</tr>
<tr>
<td>$s_a$</td>
<td>Annual survival during ammocoete phase</td>
<td>0.447$^3$</td>
</tr>
<tr>
<td>$s_T$</td>
<td>Survival during transformation phase</td>
<td>0.75</td>
</tr>
<tr>
<td>$s_P$</td>
<td>Survival during parasitic (juvenile) phase</td>
<td>0.75</td>
</tr>
<tr>
<td>$\phi$</td>
<td>Proportion of age-0 larvae that emigrate to lentic habitats</td>
<td>0.0075$^3$</td>
</tr>
<tr>
<td>$p'_{f}$</td>
<td>Proportion of females</td>
<td>0.5</td>
</tr>
<tr>
<td>$p'_{i,a,b}$</td>
<td>Proportion of larvae transforming into parasites</td>
<td>equation 7</td>
</tr>
<tr>
<td>$\tau_0$</td>
<td>Logistic transformation curve parameter</td>
<td>0.134 (upper$^3$), 0.176 (lower$^3$)</td>
</tr>
<tr>
<td>$\tau_1$</td>
<td>Logistic transformation curve parameter</td>
<td>-19.223 (upper), -23.091 (lower)</td>
</tr>
</tbody>
</table>

**Growth**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Assumed Value or Equation Where Calculated</th>
</tr>
</thead>
<tbody>
<tr>
<td>$l'_{i,a,b}$</td>
<td>Total length of larval sea lamprey for bin $b$</td>
<td>equations 4,5</td>
</tr>
<tr>
<td>$l_{i,a}$</td>
<td>Mean length-at-age of larval sea lamprey</td>
<td>equations 4,5</td>
</tr>
</tbody>
</table>
Table 1. contd…

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Assumed Value or Equation Where Calculated</th>
</tr>
</thead>
<tbody>
<tr>
<td>$d_i$</td>
<td>Duration of growing season (number of days)</td>
<td>varies by reach</td>
</tr>
<tr>
<td>$\kappa_i$</td>
<td>Brody growth parameter</td>
<td>varies by reach</td>
</tr>
<tr>
<td>$\ell_0$</td>
<td>Initial von Bertalanffy length in millimeters</td>
<td>20</td>
</tr>
<tr>
<td>$\bar{\ell}_a$</td>
<td>Mean von Bertalanffy asymptotic length (mm)</td>
<td>159.1</td>
</tr>
<tr>
<td>$\ell_{ab}$</td>
<td>Size bin-specific von Bertalanffy asymptotic length (mm)</td>
<td>equation 4</td>
</tr>
<tr>
<td>$\varepsilon_l$</td>
<td>Deviations about mean length</td>
<td>range is -2 to +2 SD</td>
</tr>
<tr>
<td>$p_{l,a,b}$</td>
<td>Proportion of larvae at age in a length bin</td>
<td>see text</td>
</tr>
<tr>
<td>CV$_l$</td>
<td>Coefficient of variation in length</td>
<td>0.08</td>
</tr>
</tbody>
</table>

**Control parameters**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Assumed Value or Equation Where Calculated</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C_i$</td>
<td>Cost of chemical control (dollars)</td>
<td>varies by reach</td>
</tr>
<tr>
<td>$\hat{E}_i$</td>
<td>Anticipated treatment effectiveness</td>
<td>varies by reach</td>
</tr>
<tr>
<td>CV$_T$</td>
<td>Coefficient of variation in assessment error</td>
<td>0.99 or 1.71</td>
</tr>
</tbody>
</table>

**Uncertainty terms**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Assumed Value or Equation Where Calculated</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\varepsilon_{l,1,t}$</td>
<td>Variance of process error in larval recruitment to age-1</td>
<td>$\sim N(0, 3.39)$</td>
</tr>
<tr>
<td>$\hat{\varepsilon}_{l,1,t}$</td>
<td>Assessment error on transformer abundance</td>
<td>$\sim$gamma</td>
</tr>
<tr>
<td>$m_{l,1,t}$</td>
<td>Mortality due to chemical control (treatment effectiveness)</td>
<td>$\sim$beta</td>
</tr>
</tbody>
</table>

1 “upper” refers to the upper Great Lakes – Superior, Michigan, and Huron
2 “lower” refers to the lower Great Lakes – Erie and Ontario
3 Lake Michigan values; different values are used for the other Great Lakes

Phase sea lampreys if other environmental factors are favorable [27, 28], and ii) the abundance of larvae in each stream reach, as sea lampreys have been shown to be attracted to a migratory pheromone released by stream-dwelling amphipods [29]. Each year, lake-wide spawning-phase sea lampreys were divided into those that migrate based on drainage area and those that migrate based on the abundance of larvae in each reach. Then, the number of spawning-phase sea lampreys allocated to a given reach was assumed to be positively related to both the drainage area and larval abundance, relative to other stream reaches:

$$S_{i,t} = S_{i,t}p_iD_i + S_{i,t}(1 - p_i)\sum L_{i,j}$$

(1)

In the simulations used in this paper, the two mechanisms were given equal weight (i.e., $p_i = 0.5$).

Recruitment of larvae was calculated from the abundance of spawning-phase sea lampreys in each stream reach using a stochastic Ricker stock-recruitment function [30, 31].

$$L_{i,0,t} = \alpha S_{i,t}p_i e^{-\frac{S_{i,t}p_i}{A_i}x_i} | S_L$$

(2)

The density-dependent term of the recruitment function depended on the area of suitable larval habitat in the stream reach, which was obtained from surveys of the length, average width and proportion of wetted area comprising two types of habitat used by larval sea lampreys: preferred (Type 1) and acceptable (Type 2). We calculated a weighted area of suitable larval habitat from:

$$A_i = v_iw_i\left(H_{i1} + H_{i2}r\right)$$

(3)

based on a conversion factor ($r$) derived from the observed ratios of sea lamprey density between these two habitat types [20]. We used lake-specific conversions based on empirical evidence of differences in this ratio among lakes (M.L. Jones, unpublished data). The other recruitment parameters for equation 2 were estimated using a meta-analysis of data from 90 stream-years of sea lamprey stock-recruitment data [31]. We chose the Ricker function to model recruitment.
because we observed reduced recruitment at high abundances of spawning-phase sea lamprey in these data. We assumed that inter-annual density-independent recruitment variation was not correlated among streams (no common “year effects”) based on empirical analyses [31]. The empirical model related abundance of spawning-phase sea lampreys to observed age-1 abundance the following year, so the number of age-0 sea lampreys in year $t$ was calculated from predicted age-1 abundance in year $t+1$ using an annual survival rate ($s_t$) assumed constant among larval ages and stream reaches.

Sea lamprey metamorphosis to the parasitic stage is governed at least in part by length [32], so we modeled the larval population as both length- and age-structured. Our approach was to consider the population as consisting of a set of different growth types, with all individuals of a given growth type being represented by a common length at age. These growth types are defined by the length bins individuals started in at age-1, and subsequent length-at-age for larval sea lamprey in a length bin ($b$) follows a von Bertalanffy growth model:

$$\ell_{i,a+1,b} = \ell_{i,a,b} + \Delta \ell_{i,a,b}$$

where $\Delta \ell_{i,a,b} = \left( \ell = b - \ell_{i,a,b} \right) \left( 1 - e^{(-b - \ell_{i,a,b})} \right)$

Nine length bins were defined, and the initial lengths and allocation of proportions of larvae to each bin were set to approximate a presumed normal distribution. The lengths associated with each length bin for age-1 were set to range from -2.0 to +2.0 standard deviations around the mean length at age-1 in increments of 0.5 for $b = 1$ to 9. Mean age-1 length was projected from a mean age-0 length, $\ell_0$, of 20 mm based on equation 4, where the mean age-0 length plays the role of $\ell_{i,a,b}$, and the assumed coefficient of variation in length at age-1, CV$_{\ell_0}$, was 0.08. Thus:

$$\ell_{i,a+1,b} = \ell_{i,a+1} \left( 1 + CV_{\ell_0} \varepsilon_b \right)$$

where $\varepsilon_b$ varies from -2.0 to +2.0 in increments of 0.5. The same distribution and calculations were applied to generate bin-specific asymptotic length parameters, $\ell_{\infty,b}$, where the mean value, $\ell_{\infty}$, was estimated from growth data for larval sea lamprey (using mark-recapture data from Treble [33]).

The remaining stream-specific parameterization of this growth model is explained in Appendix B. The true stream-specific parameters for growth are not known, so we allowed for this uncertainty in our simulations. We achieved this by using the among-stream variability in two growth rate parameters (average daily growth and growing season length) for streams reported in the ESTR database as an empirical sample of possible growth rates for each stream. We accounted for expected geographical variation in growth rates among streams tributary to a particular lake by grouping streams regionally according to spatial patterns of growth variation within a lake basin. For Lake Michigan, we assigned each stream to one of three groups: Indiana and the southern lower peninsula of Michigan; Wisconsin and the northern lower peninsula of Michigan; and the upper peninsula of Michigan. We assigned actual growth rate parameters for individual streams by randomly choosing a pair of values (sampling with replacement) for average daily growth rate and growing season length from the set of candidate pairs for the group to which the stream belonged for each simulation.

For age-1 larval sea lamprey in all stream reaches, the proportions of the total larval population falling into each bin, $\hat{p}_{i,a+1,b}$, were set to 0.04, 0.07, 0.12, 0.17, 0.20, 0.17, 0.12, 0.07, 0.04 for bins 1 to 9 respectively to approximate the desired normal distribution. For subsequent ages, $\hat{p}_{i,a,b}$ was updated to reflect losses within a bin due to metamorphosis:

$$\hat{p}_{i,a+1,b} = \frac{\hat{p}_{i,a,b} \left( 1 - \hat{p}_{i,a,b} \right)}{\sum_{b=1}^{q} \hat{p}_{i,a,b} \left( 1 - \hat{p}_{i,a,b} \right)}$$

The probability of metamorphosis for an individual larval lamprey depended on its length and was calculated for ages-2 and older:

$$p_{i,a,b} = \frac{e^{(6.9 + 4.74)} \varepsilon_{b}}{\left( 1 + e^{(6.9 + 4.74)} \varepsilon_{b} \right)}$$

The parameters for equation 7 were assumed to differ between the upper (Superior, Michigan, and Huron) and lower (Erie and Ontario) Great Lakes [23] (see Table 1). Note that the proportions $\hat{p}_{i,a,b}$ are not influenced by mortality because this rate was assumed to be the same for each length bin. The number of transformers (potential parasites) in each stream reach was then calculated across ages 2 through 6 and all 9 length bins within an age group by:

$$T_{i,t} = \sum_{a=2}^{q} \left( \sum_{b=1}^{9} \hat{p}_{i,a,b} p_{i,a,b} \right)$$

A similar sequence of calculations (equations 4-8) was used to model the population dynamics of larval sea lampreys in lentic habitats and areas not susceptible to control actions (Appendix A).

The larval population in each stream reach was updated annually by adding new recruits to age 0 (equation 2) and by subtracting losses due to natural mortality, chemical control, and metamorphosis to the parasitic stage:

$$L_{i,a+1,t+1} = L_{i,a,t} \left( 1 - \sum_{b=1}^{9} \hat{p}_{i,a,b} p_{i,a,b} \right) \left( 1 - m_{i,t} \right) s_L$$

$$a = 1, 2 \ldots 5$$

For age-1 larvae there is an additional loss term, due to outmigration of age 0 larvae to lentic areas (see Appendix A) and there are no losses due to metamorphosis:
### Table 2. Summary of the Management Strategies and Associated Levels of Two Sources of Uncertainty Implemented Using the Operating Model for Lake Michigan

<table>
<thead>
<tr>
<th>Variant</th>
<th>Management Strategy</th>
<th>Control Budget</th>
<th>Assessment CV</th>
<th>Growth Variation?</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Assessment-based</td>
<td>Base(^1)</td>
<td>Low (0.99)</td>
<td>Yes</td>
</tr>
<tr>
<td>2</td>
<td>Assessment-based</td>
<td>Base</td>
<td>Average (1.71)</td>
<td>Yes</td>
</tr>
<tr>
<td>3</td>
<td>Fixed Schedule 1</td>
<td>Base + Assessment(^2)</td>
<td>NA</td>
<td>Yes</td>
</tr>
<tr>
<td>4</td>
<td>Fixed Schedule 2</td>
<td>Base</td>
<td>NA</td>
<td>Yes</td>
</tr>
<tr>
<td>5</td>
<td>Fixed Schedule 2</td>
<td>Base</td>
<td>NA</td>
<td>No</td>
</tr>
</tbody>
</table>

\(^1\) Base control budget for Lake Michigan was $2,027 million USD

\(^2\) Assessment savings of $345,000 USD were added to the base control budget

NA = not applicable, because assessment information was not used to rank streams

\[ L_{i,1,t+1} = L_{i,0,t} (1 - m_{i,t}) s_L (1 - \phi) \]  

(10)

These equations implicitly assume that the few larvae that survive to age-6 and do not transform at that age will die and not reach older ages.

The annual number of parasites leaving larval habitat areas was calculated from the previous year’s population of transformers that survived treatment in treated areas (called residuals; see Chemical treatment below) combined with those present in untreated areas (\(j \) in equation 11):

\[ P_j = \left( \sum T_{i,j, \leq t} (1 - m_{i,t}) + \sum j T_{j,t+1} \right) s_T \]  

(11)

Finally, the total lake-wide population of adult sea lamprey in year \(t+1\) was calculated from the number of parasites surviving in year \(t\):

\[ S_{t+1} = s_p P_t \]  

(12)

### Management Strategies

We used the sea lamprey operating model to compare the performance of five management strategy variants based on two basic strategies for stream selection. We simulated the chemical treatment of streams following either an assessment-based rule generated from a transformer kill-per-dollar estimate or a fixed-treatment schedule in which the number of years between treatments for each treatable area was predetermined. For the assessment-based strategy of stream selection, we evaluated two variants with different levels of assessment uncertainty. For the fixed-treatment schedule we considered two budget options: in one variant we assumed savings from the absence of larval assessment were used to increase the chemical treatment budget (i.e., treat more streams per year); in the other variant we assumed the chemical treatment budget remained the same as for the assessment-based strategy. Finally, we also considered an additional variant in which growth uncertainty was eliminated, speculating that the assessment savings could be used to reduce this source of uncertainty. Although it is likely that some of this growth uncertainty is due to process variation which is probably not reducible, we chose to set growth uncertainty to zero for this variant to assess the maximum benefit that could be derived from reducing this source of uncertainty, analogous to an Expected Value of Perfect Information calculation [2]. Thus five different management strategy variants were considered (Table 2).

### Assessment-Based Strategy for Stream Ranking

To select stream reaches for chemical treatment based on assessment information, we simulated the annual stream ranking procedure used since 1995 in the sea lamprey control program [19]. Estimated transformer abundance (i.e., population assessment) was calculated as a function of the “true” transformer abundance:

\[ \hat{T}_{i,t} = T_{i,t} \hat{\epsilon}_{i,t} \]  

(13)

where \( \hat{\epsilon}_{i,t} \) was drawn from a gamma distribution with a mean of 1 and a CV of either 0.99 (the “low” assessment error) or 1.71 (the “average” assessment error). The two levels of assessment error represent the minimum and average CVs resulting from Monte Carlo simulations performed by Steeves [22] using assessment data from nine Great Lakes streams.

In each year of a simulation, areas available for treatment were ranked in order of treatment priority based on their relative estimated cost-effectiveness of treatment (i.e., ranked to maximize the estimated number of transformers killed per dollar of treatment cost):

\[ \frac{\hat{T}_i \hat{E}_i}{C_i} \]  

(14)

As noted earlier, this approach will yield the maximum level of suppression per dollar spent when the variables in equation 14 are known without error [21]. For ranking purposes, we used the treatment effectiveness values \( \hat{E}_i \) assumed by the GLFC in their ranking procedures. These values varied among stream reaches and ranged from 0.75 to 0.99 (proportion killed) but were constant over time. The anticipated treatment cost and effectiveness values were derived from data on previous treatments and expert judgment. We assumed treatment effectiveness in lentic habitats was 0.75 based on recorded treatment assessments for such areas.
Chemical control costs for each stream reach were obtained from recent data on lampricide costs. Control costs for lentic habitat units were fixed at $5 000 ha$^{-1}$ based on recent treatments of multiple lentic units within the St. Marys River, Lake Huron. In general, stream reaches and treatable lentic habitats with high densities of large ammocoetes (i.e., those likely to metamorphose into parasites within a year) and modest treatment costs were ranked highest. For the Lake Michigan simulations reported here, we used an annual control budget of $2.027 million for all simulations and all years when the assessment-based approach was used to rank treatment areas. Each year, reaches were treated in rank order, from highest to lowest, until the budget apportioned to lampricide control was exhausted or until remaining funds were insufficient to treat any remaining locations.

### Fixed-Treatment Schedule Strategy

We compared the assessment-based strategy to an alternative strategy that used a fixed-treatment schedule to apply chemical control to Lake Michigan sea lamprey producing streams. The fixed-treatment schedules did not rely on assessment information to rank streams for treatment, but rather used prior information on stream-specific larval growth rates to order streams according to the rate at which larval cohorts would reach a size where metamorphosis was likely. Streams with faster growth rates were treated more frequently, subject to budgetary constraints on the total number of streams that could be treated each year. We considered two fixed-treatment variants with contrasting budgets for chemical control. In 2007, $2.9$ million was spent on larval assessment in the Great Lakes basin, of which $1.38$ million was used for surveys aimed at ranking streams for treatment (G. Christie, GLFC, Ann Arbor, MI, personal communication). Lake Michigan contains approximately 25% of all treated stream reaches in the Great Lakes basin, so we assumed for the simulations reported here that 25% of the budget for stream ranking assessment ($345,000$) would have been used for the assessment of Lake Michigan streams. The control budget used for generating the first treatment schedule (Fixed Schedule 1) was the sum of the base control budget ($2.027$ million) and the reallocated assessment funds for a total control program expenditure of $2.372$ million. The second treatment schedule (Fixed Schedule 2) was generated under the assumption that additional funds would not be available to augment chemical control even if assessment for ranking streams was eliminated, and thus the control budget for this variant remained at the base amount of $2.027$ million. The variant in which we assumed growth uncertainty was eliminated was only applied to Fixed Schedule 2, based on the premise that savings from assessment would be applied to reducing growth uncertainty rather than towards increased chemical control.

Fixed-treatment schedules were designed by assigning a cycle length representing the number of years between treatments to each treatment unit (stream reach or lentic habitat unit). Stream reaches with the highest estimated annual growth rates and lentic habitat units with the highest levels of recruitment were assigned the shortest cycle lengths. The overall annual budget available for treatment, as well as the costs of treating all treatment units in Lake Michigan, determined the range of cycle lengths; on average cycle lengths were longer for Fixed Schedule 2 than Fixed Schedule 1 because the smaller budget for the former allowed fewer treatment units to be on the schedule in any particular year (Table 3). We used an iterative and by necessity somewhat ad hoc procedure to determine the cycle lengths for all stream reaches by first ordering reaches from fastest to slowest growth rates, and then varying the cycle lengths for individual streams subject to the constraints imposed by the annual treatment budget and that reaches with faster growth rates never had a longer cycle length than a stream with a slower growth rate. We did not have growth rate data for the lentic habitat units, so these areas were assigned cycle lengths ranging from 4 (highest recruitment areas) to 13 (lowest recruitment areas) years, for both budget variants. These lentic habitat units comprise a small proportion of the sea lamprey larval habitat in Lake Michigan (assumed to total less than 4%) that is available for treatment and are also believed to support lower densities of larvae than favorable stream habitats. After assigning a cycle length to each area available for treatment, we generated fixed schedules that assigned areas to actual simulation years and which minimized the annual variability in treatment budgets. In each iteration and each year, all areas scheduled for treatment were treated, and the budget required to do so was recorded. In the fixed-treatment variants, the actual amount expended on control varied from year to year based on which areas were due for treatment, but with the overall average annual expenditure set by the available budget.

### Chemical Treatment

Once an area is selected for chemical treatment, the actual treatment effectiveness is subject to a variety of influ-

<table>
<thead>
<tr>
<th>Cycle Length</th>
<th>Fixed Schedule 1</th>
<th>Fixed Schedule 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>4 years</td>
<td>14</td>
<td>0</td>
</tr>
<tr>
<td>5 years</td>
<td>37</td>
<td>14</td>
</tr>
<tr>
<td>6 years</td>
<td>38</td>
<td>67</td>
</tr>
<tr>
<td>7 years</td>
<td>3</td>
<td>11</td>
</tr>
<tr>
<td>8 years</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>9 years</td>
<td>0</td>
<td>1</td>
</tr>
</tbody>
</table>

**Table 3. The Number of Stream Reaches in Lake Michigan with Cycle Lengths of 4-9 Years for Each Fixed Treatment Schedule**
ences (e.g., discharge, changes in pH), although most stream treatments result in levels of larval mortality exceeding 90%. Therefore, if a simulated stream reach was selected for TFM treatment, the entire larval population in that area was reduced based on drawing an estimate of mortality (i.e., treatment effectiveness; \( m_{ij} \), equations 9-11) from a highly-skewed beta distribution that produced an average treatment mortality near 93% with a CV around 0.10. Little is known about the variability of treatment effectiveness in lentic habitats, although treatment of these habitats is generally considered less effective than lotic control. We assumed that actual mortality due to chemical treatment in a lentic habitat unit would vary about a mean 75% according to a normal distribution with a CV of 0.10. Treatment mortality was applied to all larvae present in the treated area, regardless of age or length (equations 9-10). For each simulation, the applied control mortality values were drawn for all locations regardless of rank status for all years, but only applied to streams that were selected for treatment. This way, treatment effectiveness values related to a single location may vary over time, but treatment effectiveness values did not vary across simulations for cases where the same location was treated in the same year.

Model Calibration and Simulations

Prior to running the simulations, the operating model was calibrated based on stream data for Lake Michigan, as well as information on both recent control expenditures (7-year mean of recent annual lampricide budgets, 1998-2004) and recent observed values of abundance for spawning-phase sea lampreys (7-year mean, 2000-2006), all provided by the GLFC. The calculations of target calibration abundance and control budget values were offset by a two-year lag to approximate an expected delay between treatments targeting larval lamprey and measures of the adult population. The goal of the calibration process was for the simulation model to approximate spawning-phase sea lamprey abundances close to recent observations when using control budgets that correspond to actual recent expenditures in Lake Michigan. The calibration budget was the combined costs associated with TFM and treatment staff (effort). Thus, the calibration budget was the same as the base control budget used during the evaluation of both management strategies. Larval survival was the primary adjusted parameter during calibration based upon earlier work [34] and because it is an important demographic parameter for which we presently have very limited information. In addition to the larval survival rate, we adjusted an outflow scalar which determined the movement of age-0 larvae from streams and the untreated habitat into lentic habitats. This outflow scalar was adjusted so that density of larvae in lentic areas was approximately one quarter of the average density in streams during the calibration runs. This target ratio was based on observed densities from a lentic inventory survey where larval lamprey densities were measured in both natal lotic areas and associated lentic habitats (Mike Steeves, Department of Fisheries and Oceans Canada, unpublished data).

To compare simulated sea lamprey abundance to the calibration target abundance, we defined the equilibrium level as mean abundance of spawning-phase sea lampreys resulting from sustained treatment. For each simulation of the calibration control budget, the simulated abundance of spawning-phase sea lampreys was averaged across the final 10 years. Then, a grand mean was also calculated by averaging across simulations. The larval survival rate was adjusted until the grand mean was approximately equal to the calibration target abundance (Fig. 3). We used 5,000 simulations with a 100 year time horizon for calibration. Once the operating model was calibrated to recent targets for Lake Michigan, alternative control variants could then be explored.
To compare policies, all simulations were also run for 100 years to allow abundance of spawning-phase sea lampreys to approach a stationary distribution of values prior to the final year of the simulation when model estimates were evaluated. Each policy was repeated 5,000 times to account for model uncertainty. For each set of 5,000 simulations, the mean abundance of spawning-phase sea lampreys was recorded for the final ten years (t = 91-100) and the grand mean was calculated across all simulations. Results for years 75-100 are also presented to display temporal trends (Fig. 4).

RESULTS

Initialization of the Operating Model and Initial Population Dynamics

Each simulation began with an initial population size of 75,000 spawning-phase sea lampreys and an age-0 larval density of 1 m⁻² based on specified larval habitat areas. These homogeneous initializations are necessary simplifications, given incomplete knowledge of age-specific abundances for sea lamprey in all Lake Michigan tributaries, and result in marked transient population dynamics during the early (first 10-15) years of a simulation. Visual inspection of temporal patterns in projected abundance indicated that stationary conditions were approached after approximately 50 years.

Comparison of Management Strategy Variants

For each management strategy variant, the treatment expenditure varied annually depending on which areas were actually treated in that year. For each fixed-treatment variant, the mean annual treatment expenditure across all years and simulations was slightly lower than, but by no more than 1.5%, of the budget expected to be available (Table 4). Annual treatment expenditures varied minimally among years for both assessment-based variants and were within 1% of the target budget.

The model was calibrated using the assessment-based strategy with the average level of uncertainty (Variant 2, Table 2); this variant best represents the status quo for management and the recent history of control on Lake Michigan. The forecasted future abundance of spawning-phase sea lampreys for this variant was 118,162 (Table 4), which is within the range of estimates of abundance from adult assessment surveys during the calibration period (85,800 – 164,700, unpublished data). The variability among simulations in this forecasted abundance is large (SD = 87,095, Table 4), reflecting the high magnitude of process uncertainty for sea lamprey recruitment.

Selecting streams for treatment using a fixed-schedule rule, but with the same overall (treatment and assessment) budget (Variant 3, Table 2), resulted in a lower forecasted mean abundance of spawning-phase sea lampreys than was seen for Variant 2. The difference was small relative to the variability in outcomes among simulations, but in 70% of cases this variant resulted in lower forecasted abundance than status quo variant (Table 4). If a fixed schedule was used without increasing the treatment budget by an amount equal to assessment savings (Variant 4, Table 2), then the average forecasted spawning-phase sea lamprey abundance was substantially higher, and the simulations almost never resulted in an instance of lower forecasted abundance than the status quo variant (Table 4, last column). As well, this strategy resulted in wide inter-annual variation in forecasted abundance (Fig. 4). For this variant, the majority of stream reaches were treated on a cycle of six years or more (Table 3), longer than the duration of the larval phase in some of these streams.
Reducing larval assessment uncertainty had a much larger effect on forecasted abundance than reducing growth uncertainty. When we repeated the assessment-based strategy but assumed a lower level of assessment uncertainty, the average forecasted abundance was approximately one-third of the baseline value (Variants 1 and 2, Table 4), and the forecasted abundance for individual simulations was nearly always lower than the status quo variant. Conversely, repeating the Fixed Schedule 2 strategy, but assuming perfect knowledge of stream-specific larval growth rates had very little effect on the outcome (Variant 5, Table 4).

**DISCUSSION**

MSE-style models have been developed for several exploited fish stocks to simulate the entire management process and to examine the effects of various types of uncertainty in fishery management [6, 35, 36]. In this paper, we describe an MSE-style operating model for sea lamprey management, in which we have incorporated a) demographic (process) uncertainty – uncertainty in larval population dynamics, b) assessment uncertainty – imperfect knowledge used for stream selection, and c) control uncertainty – variable efficacy of chemical treatments. The model can be used to examine a variety of strategic questions concerning sea lamprey control in the Great Lakes by simulating the performance of the management system while explicitly accounting for these uncertainties.

We used the sea lamprey operating model to conduct a set of simulation experiments, forecasting the average number of spawning-phase sea lampreys in Lake Michigan resulting from five variants which differed in the management strategies used for stream selection and levels of two sources of uncertainty. At current levels of assessment uncertainty, reallocation of the funds used to assess stream reaches to support their treatment based on a fixed treatment schedule resulted in a lower expected abundance of spawning-phase sea lamprey in our simulations for Lake Michigan. We note that this strategy may not be the optimal fixed-schedule for the budget available; optimizing the schedule (beyond the scope of this analysis) might yield even better performance for the same budget. In contrast, treating stream reaches on a fixed schedule with no additional resources available for chemical treatments was much less effective than selecting reaches for treatment based on larval assessment, highlighting the sensitivity of the average performance of fixed-schedule strategies to relatively small variations in budget. The most desirable outcomes were produced by the management variant with relatively low assessment uncertainty, but the costs associated with achieving this increased accuracy remain unknown.

These results raise important questions about the role of larval population assessment in sea lamprey control. We concluded that the current budget for treatment of Lake Michigan sea lamprey producing streams was only sufficient for successful control if the selection of streams was guided by an assessment program. On the other hand, comparatively small increases in funds for stream treatment (a 16% increase from current levels) were sufficient to overcome the reduced accuracy of a fixed treatment schedule. Ultimately, our results suggest that alternative strategies where less is invested in assessment deserve consideration by sea lamprey program managers. In a related empirical study, the current assessment procedure that the operating model in this paper simulates was compared to an alternative rapid assessment method [37]. This rapid assessment method can be viewed as somewhere between the two extremes simulated here (current assessment versus no assessment), and was found to outperform the current method, but only if the savings from using the rapid assessment method were applied to control, similar to Variant 3 in our simulation experiment. The Great Lakes Fishery Commission adopted the rapid assessment method in 2008. While our results could be used to argue that a strategy with no assessment program at all is viable, the absence of any assessment would limit a manager’s ability to verify the performance of the strategy and the operating model on which it is based.

Our results also highlight the particular importance of assessment uncertainty for sea lamprey management. When assessment uncertainty was reduced to the minimum level observed in Steeves [22], the assessment-based decision rule...
outperformed any other method of stream selection, despite the fact that more money was allocated to treatments under the Fixed Schedule 1 variant. Of course if assessment uncertainty were to be reduced by increasing annual assessment expenditures (i.e., more intensive population assessments), then the gains in suppression forecasted here would probably not be realized, at least absent an overall increase in the budget. However, it is possible that valuable reductions in assessment uncertainty could be achieved without increasing annual expenditures, particularly by improving the accuracy of models used to interpret assessment data. A noteworthy example of this concerns the model that is used to predict the proportion of the larval population in a stream reach that is expected to metamorphose during the year following an assessment [19]. Recent research into factors affecting sea lamprey metamorphosis has yielded a new model for forecasting metamorphosis for use in the stream ranking process that appears to be more accurate than the model currently in use [32]. Replacement of the current model with this newer model could substantially reduce the uncertainty associated with use of assessment data to rank streams for lampricide treatment.

For practical reasons all simulation tests of potential management strategies reflect choices regarding what uncertainties to address, and to what extent [10]. While we did explicitly incorporate some uncertainties, others were dealt with only through limited sensitivity analysis, and others were not quantitatively addressed. In principle Management Strategy Evaluation, to be comprehensive, should include a thorough evaluation of the robustness of the forecasted performance of each policy to all sources of uncertainty. In addition to the results for the base model presented in this manuscript, we also evaluated the same strategies using an alternative model for how sea lamprey grew. In that alternative model mean length-at-age followed a von Bertalanffy model, but the larval length distribution at each age followed a normal distribution, with no change to the distribution about the mean occurring to reflect the earlier transformation of faster growing larvae. This alternative version of the model produced very similar results to those reported here, suggesting that the specifics of among individual differences in growth are unlikely to have a strong influence on our results. We believe there remains scope for further sensitivity analysis of our sea lamprey MSE, particularly with respect to the highly influential larval survival parameter we used to calibrate our simulations.

As we have shown here, the sea lamprey operating model offers a valuable management tool for both simulating the impacts of management decisions and exploring the relative influences of various sources of uncertainty. Our simulation experiment demonstrated the large influence of assessment uncertainty on the effectiveness of management actions and the comparatively small influence of growth (process) uncertainty. In an earlier study [30], a simpler model was used to demonstrate the large influence of process uncertainty in recruitment on the relative performance of control strategies that either targeted larval populations (i.e., lampricide control) or targeted adult reproductive success (e.g., traps and sterile male releases). We have also used the operating model to compare the performance of different approaches to ranking streams for lampricide treatment based on assessment data [33], to compare control strategies that rely exclusively on chemical control of larval populations to those that utilize a mix of chemical control and methods that target adult reproductive success [31], and to determine management targets for sea lamprey control using Economic Injury Level [38] calculations [39]. Reporting the results of these applications is beyond the scope of this paper but will be the subject of future reports. Overall, we see great promise for the use of MSE-style approaches to inform fisheries management and, in this paper, present evidence that such analyses are beneficial even when management strategies are not directly focused on regulating harvest.

ACKNOWLEDGEMENTS

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Appendix A. Description of Alternative Larval Habitat Areas

In addition to stream reaches targeted by lampricide control, the operating model represented three other areas considered capable of supporting larval sea lamprey. First, some lentic areas of the Great Lakes are known to contain larval sea lampreys (called “lentic habitats” here), presumably populated by downstream emigration of larvae from nearby streams where spawning occurred. These lentic habitats can be treated, for a cost, using granular Bayluscide. Second, there are areas that we presume to be untreatable, either because they have not yet been detected by surveys or are not cost-effective to treat (“untreated habitat”). Unlike the individual stream reaches in the model, however, these two types of areas are not intended to represent specific locations, but rather general habitat types that are capable of supporting larval sea lamprey. Third, a representation of the St. Marys River was included in the operating model for simulations of Lake Huron (“river habitat”; included as 0 habitat area for the currently presented simulations of Lake Michigan). For these alternative habitat representations, demographic parameters were based on averages from the stream-specific database for that lake. It has been suggested that growth rates of larvae in lentic habitats might generally be lower than in streams, but there are no empirical data to currently justify a different growth assumption for these habitats. Finally, we simulated population assessments for individual units of the lentic habitats using the same uncertainty assumptions as described for the stream reaches. There is no reason to expect larval density estimates for these habitats would differ in precision from those for stream habitat.
The total area of lentic habitats for each Great Lake was estimated by sea lamprey biologists and managers (T.B. Steeves, M. Fodale, and J. Slade, unpublished data). We simulated the annual colonization of lentic habitats by assuming that a small fraction of the age-0 production emigrates from all streams to lentic habitats. We adjusted this fraction during model calibration, such that the resulting average density of lentic-dwelling larvae was approximately 25% of the average larval density in streams, based on limited data on stream/lentic habitat density ratios for 11 Great Lakes streams (T.B. Steeves, DFO, unpublished data).

This approach to colonizing lentic habitats is clearly a simplification, in that not all streams actually contribute larval to lentic habitats and there is likely emigration of larvae older than age-0. However, there are few if any data to support a more realistic representation at this time, and we felt that the key requirement was to connect lentic recruitment to stream production generally, rather than developing a spatially explicit model of stream-lentic connections. Further exploration of the significance of this simplification to our model may be warranted in the future, particularly if the treatment of lentic habitats becomes an important component of Great Lakes sea lamprey control.

Once age-0 sea lampreys were allocated to the overall lentic habitat for a lake, they were distributed among individual lentic habitat units based on observations of the distribution of larvae among lentic-type habitats in the St. Marys River. We used data from 25 St. Marys River plots that had larval abundance estimates to define a relationship between the cumulative area of plots (x) and the cumulative proportion of the total larval population (y) in all plots and fitted the following function to these data:

\[
y = \frac{1 - e^{-\lambda x}}{1 - e^{-\lambda}}
\]  
(A1)

where \( \lambda \) describes the extent to which the majority of the larvae are in a small proportion of the total area, with larger values implying a less uniform distribution among units.

The number of individual lentic habitat units (N) was determined based on dividing the total lentic area for a lake by an average size calculated for 56 lentic treatment units (plots) in the St. Marys River that were considered for treatment during 2006 (12.5 ha; Gavin Christie, GLFC, unpublished data). During each year of a simulation, we distributed the age-0 larvae allocated to treatable lentic habitat among the N individual lentic units as:

\[
L_{i,0,t} = \begin{cases} 
L_{0,0} \cdot \left(1 - e^{-\lambda x_i}\right) / \left(1 - e^{-\lambda}\right), & \text{if } i = 1 \\
L_{0,0} \cdot \left(1 - e^{-\lambda x_i}\right) / \left(1 - e^{-\lambda}\right) - \sum_{j=1}^{i-1} L_{j,0,t}, & \text{for } i = 2 \text{ to } N
\end{cases}
\]

(A2)

where \( L_{0,0} \) is the total number of age-0 larvae allocated to the lentic habitat for a given year t, and \( x_i \) is the proportion of total lentic area in units 1 through i, and \( \lambda \) was 3.02 based on the fit of equation A1. Once calculated, the proportion of larvae allocated to an individual lentic unit was held constant for all simulation years. Next, we assumed that the treatment costs for individual lentic units would be comparable to recent costs for actual treatment of St. Marys River plots ($5000 ha\(^{-1}\); Gavin Christie, unpublished data). Thus, the simulated individual lentic units were of equal size and had equal treatment cost per area but varied in larval density.

The contribution of untreated habitats to parasitic sea lamprey production in the Great Lakes is unknown. Based on the expert opinion of sea lamprey control program biologists and managers, we fixed the area of untreated larval habitat at 2% of the total area of the total larval habitat in streams for each lake. We assumed, in effect, that larval densities in these untreated habitats were comparable to those in stream larval habitats. These untreated habitats contributed the same proportion of their age-0 larval production to lentic habitats each year as was contributed from stream reaches.

Appendix B. Parameterization of the von Bertalanffy Larval Growth Model for Sea Lamprey Based on Stream-Specific Growth Parameters Originally Developed for a Linear Growth Model

This appendix describes how the stream-specific parameters used in the von Bertalanffy model (equation 4) were obtained based on information already available in the ESTR database [19]. The stream-specific growth rates in ESTR were determined originally for use in a linear growth model. For each Great Lake, the previously assembled data included stream-specific estimates of both the duration of the growing season (\( d_i \)), in days, and the average daily growth rate (\( G_i \)), and had been used to predict mean length at age for stream \( i \) based on:

\[
\ell_{a,i} = ad_i G_i + \ell_0
\]  
(B1)

where \( a \) is age, and \( \ell_0 \) is a user-specified length at age-0 (20 mm). Recent information suggests that growth of larval sea lampreys is asymptotic [33]. Therefore, a von Bertalanffy growth model would likely provide a better representation of length at age for larval sea lamprey. Thus we describe a method by which existing stream-specific database values (\( d_i \) and \( G_i \)) derived for a linear growth model, could be used to specify stream-specific parameters in a non-linear growth model.

As with the linear growth model, the time available for growth can be represented by \( a \) and \( d_i \), which both can be directly incorporated into a nonlinear model. However, the linear-model form of the stream-specific daily growth rate (\( G_i \)) cannot simply be inserted into the exponent of the non-linear model. Therefore, we scaled the stream-specific values of \( G_i \), recorded in the existing database, to serve as the Brody growth parameter (\( k_i \)) in the von Bertalanffy model using an assumption about a reference point. The selected reference point was the length at which 50% of larval sea lamprey would be expected to metamorphose (\( \ell_r \)) and was
specific to the transformation curve (specific to either the upper or lower Great Lakes).

By assuming that $\ell_T$ should be reached at the same age regardless of which growth model is chosen, we can solve for a relationship between $k_i$ and $G_i$:

$$k_i = \frac{\ln \left( \frac{\ell_T - \ell_a}{\ell_0 - \ell_a} \right)}{G_i} \quad (B2)$$

such that $k_i$ is directly proportional to $G_i$. This assumption suggests that the parameters for the original linear growth model were relevant because they produced length-at-age values which in turn produced a realistic pattern of transformation-at-age. In other words, both the linear model (equation B1) using $G_i$ and the von Bertalanffy model (equation 4) using $k_i$ should produce $\ell_T$ at precisely the same age.

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